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## Evaluation of Cell Parameters of TN Liquid Crystal Cells by using a Stokes Parameter Method

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Evaluation of cell thickness and a twist angle of a liquid crystal layer is very important in the liquid crystal study and manufacturing. We have developed an analysis system of the cell thickness and the twist angle of the liquid crystal layer, named 'LCD Analyzer', which is based on the Stokes Parameter Method. We have examined the effects of the performance of the optics on the measurement and a measuring condition, and achieved good precision of evaluating the cell parameters.

**Keywords:** TNLCD; cell thickness; twist angle; Stokes Parameter Method

### INTRODUCTION

Cell thickness and twist angle of a liquid crystal (LC) layer are the most important parameters in a twisted nematic (TN) liquid crystal display (LCD). Recently, the Stokes Parameter Method (SPM) has been proposed by Zhou *et al.* [1] for evaluating the cell thickness and the twisted angle of the LC layer. The SPM is very simple technique because only 4 transmitted monochromatic light intensities with different optics setup are needed. But precision of evaluating the cell

parameters is not good in some cases.

In this paper, we examined the effects of the performance of the optics used on the SPM measurement, and determined practical specifications of the optics. According to this result, we have developed the analysis system of the cell thickness and the twist angle of the LC layer, named 'LCD Analyzer', which is based on the SPM. The cell thickness and the twist angle can be measured simultaneously. Moreover, 2 dimensional distribution of these parameters can be measured by using a CCD camera. It is also possible to calculate the anchoring energy from the measured parameters. In this paper, we also demonstrate a specification of the LCD Analyzer and an example of the measurement (the dependence of the twist angle on the cell thickness was measured).

## THEORY

In this section, we summarize the outline of the SPM measurement [1,2]. The Stokes parameters of the polarization through the TN cell normalized by the incident light intensity are written as a function of the cell thickness  $d$  and the twist angle  $\phi$ .

$$S_0 = a_1^2 + a_2^2 + b_1^2 + b_2^2 = 1 \quad (1)$$

$$S_1 = b_1^2 - a_1^2 - a_2^2 \cos 4\alpha + b_2^2 \cos 4\alpha + 2a_2b_2 \sin 4\alpha \quad (2)$$

$$S_2 = 2a_1b_1 + (b_2^2 - a_2^2) \sin 4\alpha - 2a_2b_2 \cos 4\alpha \quad (3)$$

$$S_3 = 2b_1(b_2 \sin 2\alpha - a_2 \cos 2\alpha) - 2a_1(a_2 \sin 2\alpha + b_2 \cos 2\alpha) \quad (4)$$

$$a_1 = \frac{1}{\sqrt{1+u^2}} \sin \phi \sin(\sqrt{1+u^2}\phi) + \cos \phi \cos(\sqrt{1+u^2}\phi) \quad (5)$$

$$a_2 = \frac{u}{\sqrt{1+u^2}} \cos \phi \sin(\sqrt{1+u^2}\phi) \quad (6)$$

$$b_1 = \frac{1}{\sqrt{1+u^2}} \cos \phi \sin(\sqrt{1+u^2}\phi) - \sin \phi \cos(\sqrt{1+u^2}\phi) \quad (7)$$

$$b_2 = \frac{u}{\sqrt{1+u^2}} \sin \phi \sin(\sqrt{1+u^2}\phi) \quad (8)$$

$$w = \left(\frac{n_e}{n_o}\right)^2 - 1 \quad (9) \quad u = \frac{\pi d}{\lambda \phi} \left( \frac{n_e}{\sqrt{1+w \sin^2 \theta_s}} - n_o \right), \quad (10)$$

where  $n_o$  and  $n_e$  are indices of the ordinary and extraordinary light of LC material, respectively,  $\lambda$  is the wavelength of the incident light,  $\theta_s$  is the pretilt angle,  $d$  is the cell thickness,  $\phi$  is the twist angle, and  $\alpha$  is the azimuthal angle of the incident director of the LC layer.

Under a laboratory coordinate shown in FIGURE 1, the normalized Stokes parameters are determined experimentally as follows.

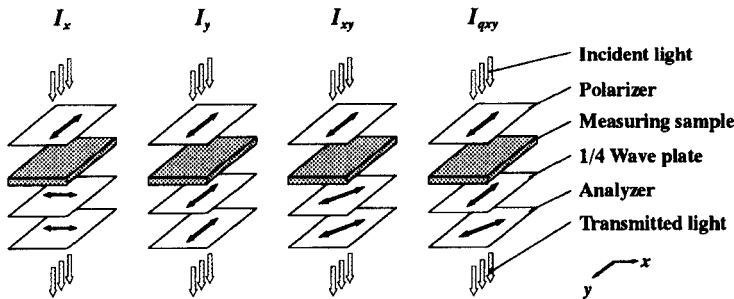
$$S_0 = (I_x + I_y) / (I_x + I_y) = 1 \quad (11)$$

$$S_1 = (I_x - I_y) / (I_x + I_y) \quad (12)$$

$$S_2 = [2 I_{xy} - (I_x + I_y)] / (I_x + I_y) \quad (13)$$

$$S_3 = -[2 I_{qxy} - (I_x + I_y)] / (I_x + I_y) , \quad (14)$$

where  $I_x$  is the transmitted light intensity when the fast axis of the wave plate and the transmission axis of the analyzer are along the  $x$  axis,  $I_y$  is when the both axes along the  $y$  axis,  $I_{xy}$  is when the both axes along a bisector of the  $x$  and the  $y$  axis, and  $I_{qxy}$  is when the wave plate axis is along the  $x$  axis and the analyzer axis is along the bisector of the  $x$  and the  $y$  axis.

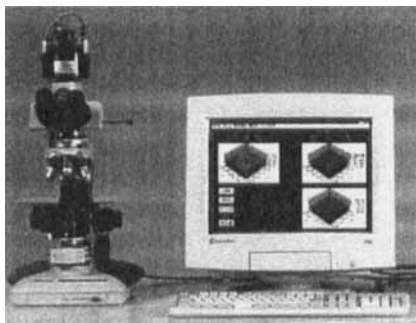


**FIGURE 1** Schematic figures of the optics setup for measuring the Stokes Parameters

After measuring  $I_x$ ,  $I_y$ ,  $I_{xy}$  and  $I_{qxy}$ , we can calculate the normalized Stokes parameters by using Equations (11~14) and evaluate  $d$  and  $\phi$  by fitting the measured Stokes parameters to Equations (1~4).

## SPECIFICATIONS

The photograph of measurement system is shown in FIGURE 2, and system diagram is shown in FIGURE 3.



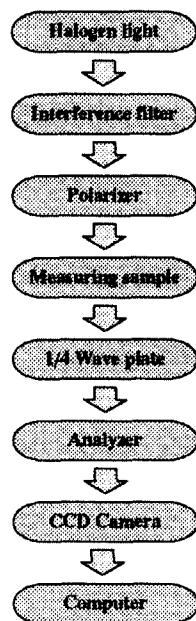
**FIGURE 2** Photograph of the LCD Analyzer

Since the flicker of the light source causes the experimental error, the high-stable type light source is used in the LCD Analyzer. The deviation of the light intensity is less than 1 %. We simulated the influence of the 1 % flicker on the evaluation of  $d$  and  $\phi$  as shown in

FIGURE 4.  $d$  is evaluated within the range of  $\pm 0.05 \mu\text{m}$  and  $\phi$  is evaluated within the range of  $\pm 0.5$  degree at the worst.

FIGURE 5 shows the simulated dependence of the transmitted light intensity on the wavelength of the light. Only  $I_{\text{qny}}$  shows small dependence, but the effect of this dependence can be neglected by using the interference filter with narrow width. In the LCD Analyzer, the full width at half maximum (FWHM) of the interference filter is less than 10 nm.

The extinction ratio of the polarizer and the analyzer also affects the reliability of the measurement. In the LCD Analyzer, the polarizer



**FIGURE 3** System diagram

and the analyzer with high extinction factor less than  $10^{-4}$  are used.

According to the above discussion, the specifications of the optical components used in the LCD Analyzer were determined as shown in TABLE 1.

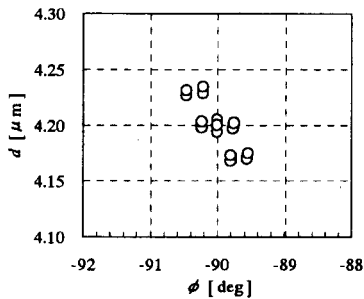


FIGURE 4 The scatter chart by the light intensity deviation 1 %

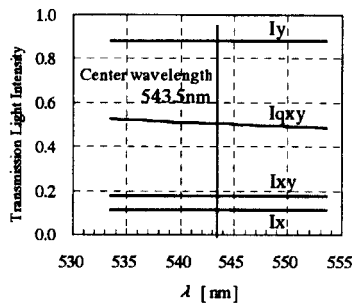


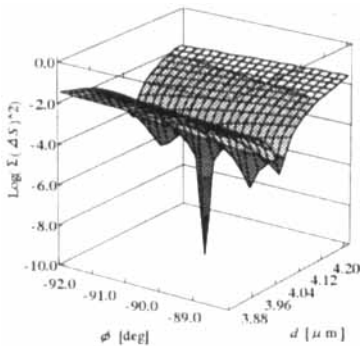
FIGURE 5 Dependency of the light wavelength

TABLE 1 Optical component specifications

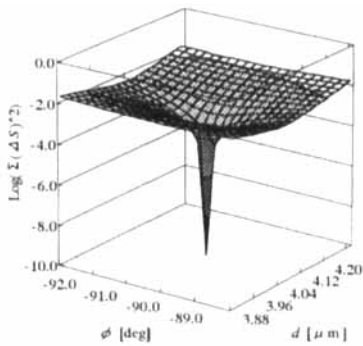
| Item                   | Specifications  |
|------------------------|---|
| 1. Light source        | Halogen light source 12V 100W<br>Color temperature 3100K<br>with intensity adjustment mechanism |
| 2. Interference filter | $\lambda = 546\text{nm}$ FWHM 10nm or less  |
| 3. Polarizer           | Extinction factor $10^{-4}$ or less   |
| 4. Wave plate          | 1/4 Wave plate ( $\lambda = 546\text{ nm}$ )  |
| 5. Analyzer            | Extinction factor $10^{-4}$ or less   |
| 6. Detector            | Full frame type Cooling-High-step-<br>CCD-Camera (16bit-output (65,535 steps))                  |

FIGURE 6 and 7 show the calculated logarithmic value of variance between the Stokes parameters of a designed TN cell ( $d = 4\mu\text{m}$ ,  $\phi = -90$  degree) and of a hypothetical cell having arbitrary  $d$  and  $\phi$

(coordinates of figures) in given  $\alpha$ 's. In the case of  $\alpha = 60$  degree (FIGURE 6), some local minimums are observed. This is the reason that the precision of evaluating the cell parameters by the SPM is not good in some special cases. To avoid this problem, the LCD Analyzer has a sample rotation stage. Therefore the LCD Analyzer achieves good precision of evaluating the cell parameters by the SPM.



**FIGURE 6** Potential curve  
( $\alpha = 60$  degree)



**FIGURE 7** Potential curve  
( $\alpha = 10$  degree)

The LCD Analyzer can measure the cell thickness, twist angle and the anchoring energy of TNLCD, (TFTLCD), STNLCD, and so on. Moreover the LCD Analyzer can measure and display the 2 dimensional distribution of these parameters by using the CCD camera.

**EXAMPLE OF MEASUREMENT**

The flow diagram of the SPM measurement by using the LCD Analyzer is shown in FIGURE 8. We measured 3 TN cells, which had different cell thickness with each other and were made by the same rubbing process. The designed parameters are listed in TABLE 2. The measurements were carried out at 3 points in each cell (here calling A-1, A-2, A-3, and so on).



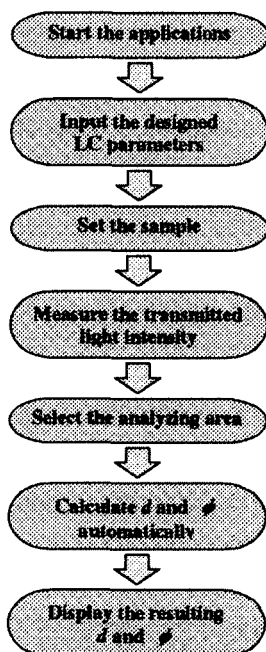
**TABLE 2** Designed data of the samples

| Sample | $d$ [ $\mu$ m] | $\phi$ [deg] | $\theta_s$ [deg] |
|--------|----------------|--------------|------------------|
| A      | 3.9            | -90          | 5                |
| B      | 4.9            | -90          | 5                |
| C      | 6.3            | -90          | 5                |

The obtained results are listed in TABLE 3 and shown in FIGURE 9. The measurements are performed at the angle  $\alpha$  of -72 degree (Sample A), -54 degree (B), 88 degree (C).

Solid and dotted curves in FIGURE 9 represent the theoretical curves of dependence of the twist angle  $\phi$  on the cell thickness  $d$  with different anchoring energies.

The tendency that  $\phi$  becomes smaller with decreasing  $d$  is clearly observed, as predicted theoretically. The anchoring energy was evaluated by  $2.0 \times 10^{-4}$  N/m, which is consistent with the strong rubbing case. These results show good measurement precision of the LCD Analyzer.



**FIGURE 8** Measurement flow diagram

**TABLE 3** Sample measurement results

| Sample | $d$ [ $\mu$ m] | $\phi$ [deg] |
|--------|----------------|--------------|
| A-1    | 3.94           | -88.1        |
| A-2    | 3.95           | -88.8        |
| A-3    | 3.96           | -88.0        |
| B-1    | 4.82           | -89.0        |
| B-2    | 4.92           | -89.4        |
| B-3    | 4.85           | -88.9        |
| C-1    | 6.34           | -89.9        |
| C-2    | 6.32           | -89.9        |
| C-3    | 6.30           | -89.5        |

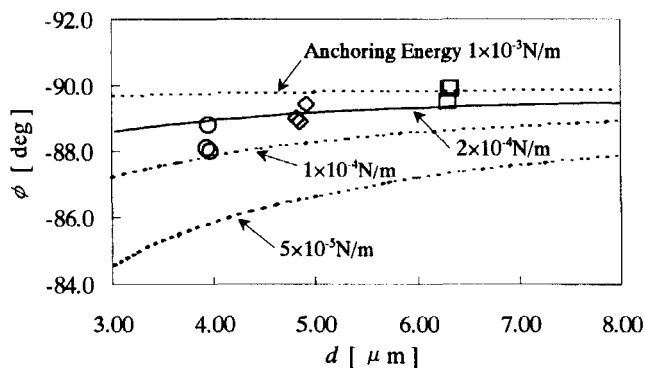


FIGURE 9 Relationships between  $d$  and  $\phi$

## CONCLUSION

We have developed the analysis system of the cell thickness and the twist angle of the liquid crystal layer, named 'LCD Analyzer', which is based on the Stokes parameter method. The Stokes parameter method is very simple technique because the only 4 transmitted monochromatic light intensities with different optics setup are needed.

By examining the effects of the performance of the optics on the measurement and a measuring condition, the LCD Analyzer can measure the cell thickness and the twisted angle with good precision. We demonstrated the simultaneous measurement of the cell thickness and the twist angle by using the LCD Analyzer, and the dependence of the twist angle on the cell thickness, *i.e.*, the twist angle becomes smaller with decreasing the cell thickness, was clearly observed. The obtained anchoring energy of  $2.0 \times 10^{-4}$  N/m is consistent with the strong rubbing case.

## References

- [1] Y. Zhou, Z. He and S. Sato: Jpn. J. Appl. Phys. **36** (1997) 2670.
- [2] Z. He, Y. Zhou and S. Sato: IDW'97 LCT 2-3 (1997) 53. Jpn. J. Appl. **37** (1998) 1982.